

Factors Affecting the Accuracy of the Recording Day Session 3a-b Estimation of carryover in automatic milking systems based on farm tests by ICAR test centres

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## Milk sampling in an AMS during an ICAR farm test

- AMS and sampler combination
- Taking the device sample
- Taking the reference sample
- What can go wrong
  - Homogenisation
  - Carryover





# Modelling carryover in an AMS - prerequisites

- Farms: usually two with at least one AMS box each
- Sampling devices depending on the requested combinations, usually two per combination
- 50 milkings per farm and day, ideally tracking cow IDs
- Device sample (usually one per milking)
  - All samples are the same size/volume
  - Sample volume does not depend on milk yield
- Reference samples (usually two per milking calculate mean)
- Get milk sample data from the milk laboratory
  - Relevant for ICAR farm test: fat content
  - But we might be interested in additional components ...



# The (basic) statistical look at carryover

$$y_i = \mu + \beta_1 f_t + \beta_2 f_{t-1} + \varepsilon_i$$

- $y_i$ : observed fat content in the sampler at  $i^{th}$  milking
- μ: intercept
- $\beta_1$ : estimated regression coefficient for current reference fat content
- f<sub>t</sub>: current reference fat content at milking t
- $\beta_2$ : estimated regression coefficient for previous reference fat content
- f<sub>t-1</sub>: previous reference fat content at milking t-1
- $\epsilon_i$ : random residual for  $i^{th}$  milking, homoscedasticity, N(0, $\sigma$ )
- Add random effects for farm, sampler, cow, repeated measures ...



# Example: carryover estimations based on ICAR farm test setups for different AMS

| Device Farms |   | Boxes<br>and | Milkings       | Cow<br>effect | Intercept | Reference             |        | Previous reference    |        | SP(POW)           | Carryover (calculated) |
|--------------|---|--------------|----------------|---------------|-----------|-----------------------|--------|-----------------------|--------|-------------------|------------------------|
|              |   | samplers     |                | included      |           | Estimated coefficient | Pr > F | Estimated coefficient | Pr > F |                   |                        |
| Α            | 1 | 2; 2         | 48; 45         | YES (sim.)    | n.s.      | 0.5965                | <.0001 | 0.2674                | 0.0006 | 0.2185            | 31%                    |
| Α            | 1 | 2; 2         | 48; 45         | NO            | n.s.      | 0.5996                | <.0001 | 0.2754                | <.0001 | 0.1201            | 31%                    |
| В            | 1 | 1; 2         | 50; 50         | YES (sim.)    | n.s.      | 0.9664                | <.0001 | 0.02077               | n.s.   | 0.1284            | 2%                     |
| В            | 1 | 1; 2         | 50; 50         | NO            | n.s.      | 0.9633                | <.0001 | 0.02735               | n.s.   | 0.1249            | <mark>3</mark> %       |
| C (1)        | 2 | 2; 1         | 67; 50         | YES           | n.s.      | 1.0153                | <.0001 | 0.004603              | n.s.   | 0.6302;<br>0.1442 | 0%                     |
| C (1)        | 2 | 2; 1         | 67; 50         | NO            | n.s.      | 1.0213                | <.0001 | -0.0007               | n.s.   | 0.2392;<br>0.1451 | 0%                     |
| C (2)        | 2 | 2; 2         | 50; 51; 50; 50 | YES           | n.s.      | 0.9992                | <.0001 | 0.003264              | n.s.   | 0.1095;<br>0.1014 | 0%                     |
| C (2)        | 2 | 2; 2         | 50; 51; 50; 50 | NO            | n.s.      | 0.9992                | <.0001 | 0.003265              | n.s.   | 0.1095;<br>0.1014 | 0%                     |



### Can we trust the results?

- Are up to 200 milkings enough to reliably estimate carryover?
- Actually: 100 milkings per AMS box, or 50 milkings per AMS/sampler combination
- Are the results repeatable?
- Which range of carryover can I detect with that test setup?
- How accurately can I determine the carryover?

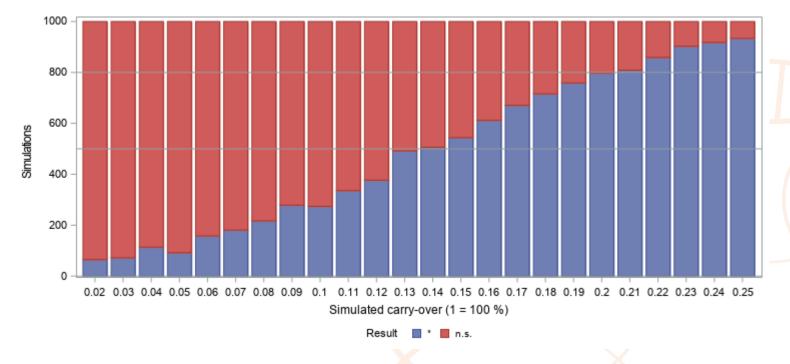


### Setting up a statistical simulation

- Create simulated milkings:
  - Generate list of cows with their milkings (also include farms or different samplers if necessary)
  - Create reference fat contents based on statistical distribution (random number from mean and standard deviation for fat in a herd)
  - Calculate device fat content by applying a carry-over effect: e.g. 0.85 times reference + 0.15 times previous reference results in new mean to randomize sample fat content from for a carry-over of 15 %
- Do this for your intended range of carry-over (e.g. 2% to 25 % in steps of 1 %)
- Run the statistical model with this simulated data set for a couple times, depending on capacity (I tried to get at least 200 runs in per variant)

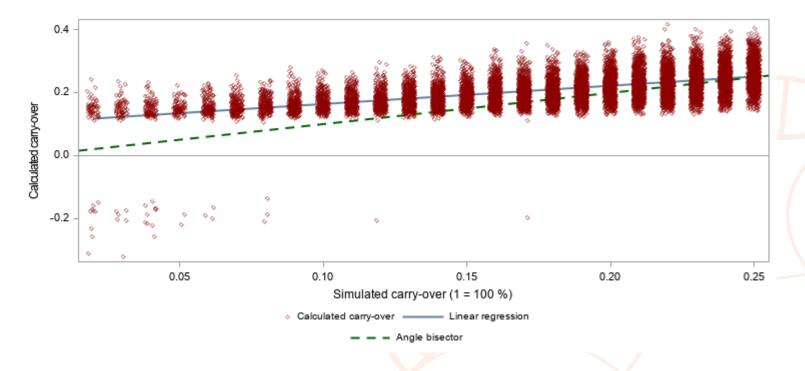


#### Results for farm test simulation with fat content (Power)





#### Results for farm test simulation with fat content (calculated carry-over)





#### First conclusion

- Results are not looking great
- Reliable estimates for a significant influence cannot be expected for carry-over below 20 % in this setup
- Carry-over is overestimated for low actual carry-over, and there seems to be a pattern
- We need to try something else!



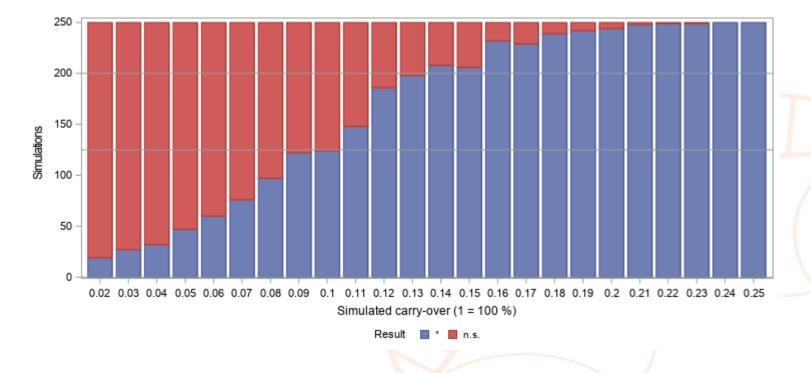
## Using additional data

- Add data from other milk components (e.g. protein, lactose ...)
- When AMS milk is well homogenized, carryover should be the same for all components
- Adjust statistical model to include more components
   (statistically not quite correct as these are no true repetitions,
   but we should get a good idea if the procedure improves)
- Updated formula introduces component c with j levels:

$$y_{ij} = \mu + c_j + \beta_1 \begin{pmatrix} f \\ p \\ l \end{pmatrix}_t + \beta_2 \begin{pmatrix} f \\ p \\ l \end{pmatrix}_{t-1} + \varepsilon_{ij}$$

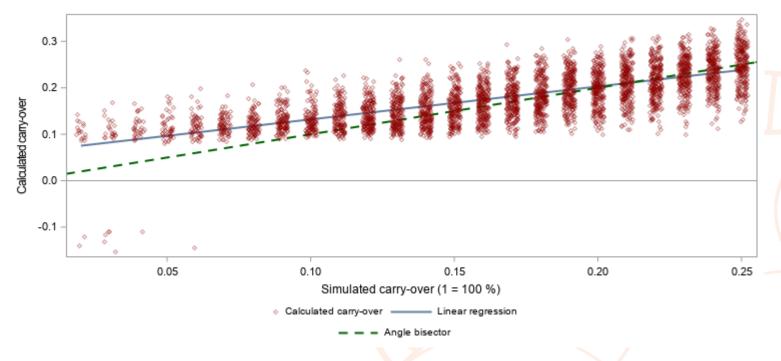


#### Results for farm test simulation with fat and protein contents (Power)



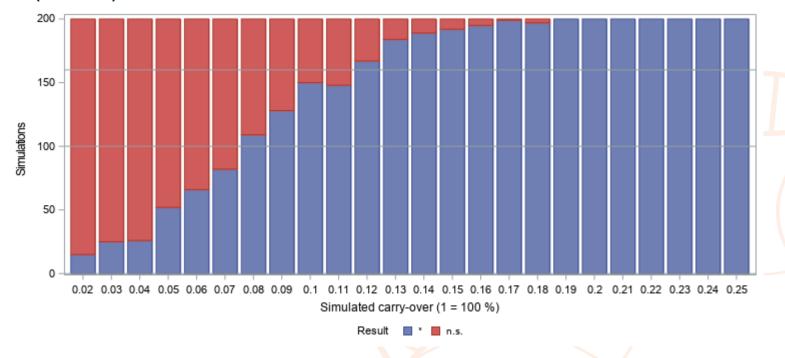


# Results for farm test simulation with fat and protein contents (calculated carry-over)



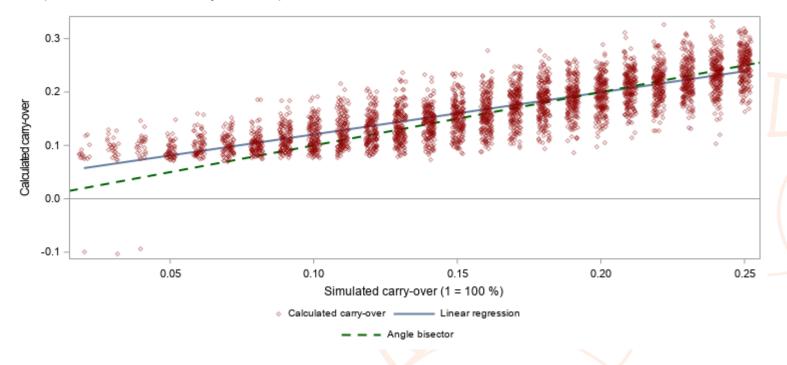


# Results for farm test simulation with fat, protein and lactose contents (Power)





# Results for farm test simulation with fat, protein and lactose contents (calculated carry-over)





#### Conclusion

- Running a statistical model with different farm test setups provided comprehensible results for carry-over estimates
- Impact of cow effect seems low and could maybe be neglected
- Power calculations show that adding more components will improve reliability of these estimates
- Methodically it is not the correct way to treat additional milk components as repetitions, but it gets the job done



### Outlook

- Check the simulation setup to find the source of the pattern in the calculated carry-over
- Switch to a multivariate statistical model that treats the different components correctly
- Begin to set up models for conventional milk meters in parlours, including the case that carry-over depends on milk yield
- Run the carry-over estimation on more data from previous ICAR farm tests





# Thanks for the interest.

Contact in case of further questions:

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